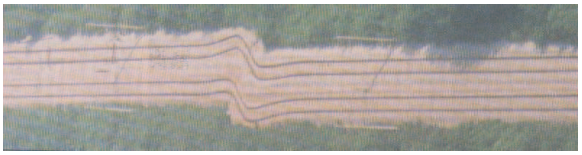
Earthquake and Volcano Deformation



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Contents

1 Deformation, Stress, and Conservation Laws **11**

1.1 Strain . . . 13

1.1.1 Strains in Curvilinear Coordinates . . . 20

1.2 Rotation . . . 21

1.3 Stress . . . 26

1.4 Coordinate Transformations . . . 29

1.5 Principal Strains and Stresses . . . 32

1.6 Compatibility equations . . . 34

1.7 Conservation Laws . . . 35

1.7.1 Equilibrium equations in curvilinear coordinates . . . 37

1.8 Constitutive Laws . . . 38

1.9 Reciprocal Theorem . . . 41

2 Dislocation Models of Strike Slip Faults **47**

2.1 Full Space Solution . . . 48

2.2 Half Space Solution . . . 53

2.2.1 Coseismic Faulting . . . 55

2.2.2 Interseismic Deformation . . . 56

2.2.3 Postseismic Slip . . . 59

2.3 Distributed Slip . . . 60

2.4 Application to the San Andreas and Other Strike Slip Faults . . . 61

2.5 Displacement at Depth . . . 67

2.6 Summary . . . 68

3 Dip Slip Faults and Dislocations in Three Dimensions **71**

3.1 Volterra's Formula . . . 73

3.1.1 Body Force Equivalents and Moment Tensors . . . 74

3.2 Screw Dislocations . . . 79

3.3 Two Dimensional Edge Dislocations . . . 81

3.3.1 Dipping Fault . . . 85
3.4 Coseismic Deformation Associated with Dipping Faults . . . 91
3.5 Displacements and Stresses due to Edge Dislocation at Depth . . . 97
3.6 Dislocations in three dimensions . . . 103
3.6.1 Full Space Green's Functions . . . 103
3.6.2 Half-Space Green's Functions . . . 104
3.6.3 Point Source Solutions . . . 106
3.6.4 Finite rectangular sources . . . 108
3.6.5 Examples . . . 110
3.6.6 Distributed Slip . . . 116
3.7 Strain Energy Change due to Faulting . . . 117
3.8 Problems . . . 118
3.9 References . . . 120

4 Crack Models of Faults **123**
4.0.1 Inversion of the Integral Equation . . . 128
4.1 Displacement on Earth's Surface . . . 130
4.2 A Brief Introduction to Fracture Mechanics . . . 130
4.3 Non Singular Stress Distributions . . . 138
4.4 Comparison of Slip Distributions and Surface Displacements . . . 140
4.5 Boundary Element Methods . . . 144
4.6 Fourier Transform Methods . . . 145
4.7 Some Three Dimensional Crack Results . . . 148
4.8 Problems . . . 149
4.9 References . . . 150

5 Elastic Heterogeneity **155**
5.1 Long Strike-Slip Fault Bounding Two Media . . . 155
5.2 Strike-Slip Fault Within a Compliant Fault Zone . . . 158
5.3 Strike-Slip Fault Beneath a Layer . . . 165
5.4 Strike-Slip Within a Layer over Half-space . . . 170
5.5 Propagator Matrix Methods . . . 172
5.5.1 The Propagator Matrix for Antiplane Deformation . . . 176
5.5.2 Vertical Fault in a Homogeneous Half-Space . . . 177
5.5.3 Vertical Fault Within Half-Space Beneath a Layer . . . 178
5.5.4 Vertical Fault in Layer over Half-Space . . . 181
5.5.5 General solution for an arbitrary number of layers . . . 183
5.5.6 Displacements and Stresses at Depth . . . 184
5.5.7 Propagator Methods for Plane Strain . . . 185
5.6 Propagator Solutions in Three Dimensions . . . 191

5.7 Approximate Solutions for Arbitrary Variations in Properties . . . 195
5.7.1 Variations in Shear Modulus . . . 199
5.7.2 Screw dislocation . . . 200
5.7.3 Edge dislocation . . . 201
5.8 Effects of Elastic Heterogeneity on Inversions . . . 205
5.9 Problems . . . 207
5.10 References . . . 208

6 Postseismic Relaxation 211
6.1 Elastic Layer over Viscous Channel . . . 214
6.2 Visco-Elasticity . . . 220
6.2.1 Correspondence Principle . . . 223
6.3 Strike-slip Fault in an Elastic Plate overlying a Viscoelastic Half-space . . . 224
6.3.1 Stress in Plate and Half-Space . . . 231
6.4 Strike Slip Fault in Elastic Layer Overlying a Viscoelastic Channel . . . 231
6.5 Dip Slip Faulting . . . 236
6.5.1 Examples . . . 240
6.6 Three Dimensional Calculations . . . 241
6.7 Concluding Remarks . . . 242
6.8 References . . . 246
6.9 Problems . . . 247

7 Volcano Deformation 249
7.1 Spherical Magma Chamber . . . 252
7.1.1 Center of Dilatation . . . 258
7.1.2 Volume of the uplift, magma chamber, and magma . . . 262
7.2 Ellipsoidal Magma Chambers . . . 265
7.3 Magmatic Pipes and Conduits . . . 277
7.4 Dikes and Sills . . . 281
7.4.1 Crack models of dikes and sills . . . 284
7.4.2 Surface Fracturing and Dike Intrusion . . . 289
7.5 Other Magma Chamber Geometries . . . 291
7.6 Viscoelastic Relaxation Around Magma Chambers . . . 295
7.7 Problems . . . 303
7.8 References . . . 307

8 Topography and Earth Curvature 309
8.1 Scaling Considerations . . . 313
8.2 Implementation Considerations . . . 315
8.3 Center of Dilatation beneath a volcano . . . 316

8.4 Earth's Sphericity . . . 318
8.5 Summary . . . 321
8.6 Problems . . . 323
8.7 References . . . 324

9 Gravitational Effects 323
9.1 Non-dimensional Form of Equilibrium Equations . . . 326
9.2 Inclusion in propagator formulation . . . 330
9.3 Surface Gravity Approximation . . . 331
9.4 Gravitational effects in viscoelastic solutions . . . 333
9.4.1 Incompressible Half-Space . . . 335
9.4.2 No Buoyancy Approximation . . . 337
9.4.3 Wang approach . . . 337
9.4.4 Comparison of Different Viscoelastic Models . . . 338
9.4.5 Relaxed Viscoelastic Response . . . 342
9.5 Changes in Gravity Induced by Deformation . . . 344
9.5.1 Gravity Changes and Volcano Deformation . . . 349
9.5.2 An Example . . . 353
9.6 Problems . . . 355

10 Poroelastic Effects 359
10.1 Constitutive Laws . . . 362
10.1.1 Macroscopic Descriptions . . . 363
10.1.2 Micromechanical Description . . . 366
10.2 Field Equations . . . 368
10.3 Analogy to Thermoelasticity . . . 371
10.4 One Dimensional Deformation . . . 372
10.4.1 Step Load on the Free Surface . . . 373
10.4.2 Time varying fluid load at the free surface . . . 375
10.5 Dislocations in Two Dimensions . . . 376
10.6 Inflating Magma Chamber in a Poroelastic Half-Plane . . . 379
10.7 Cummulative Poroelastic Deformation in Three Dimensions . . . 386
10.8 Solution when pore pressure distribution is known . . . 391
10.9 References . . . 396
10.10Exercises . . . 397

11 Fault Friction 401
11.1 Slip Weakening Friction . . . 403
11.2 Velocity Weakening Friction . . . 405
11.3 Rate and State Friction . . . 406

11.4 Linearized Stability Analysis . . . 416
11.5 Implications for earthquake Nucleation . . . 419
11.5.1 Spring-Slider Stick Slip Cycles . . . 422
11.6 Non-linear stability analysis . . . 430
11.7 Afterslip . . . 433
11.8 Transient Slip Events . . . 439
11.9 Concluding Remarks . . . 440
11.10Problems . . . 441
11.11References . . . 442

12 Interseismic Deformation and Plate Boundary Cycle Models 445
12.1 Elastic Dislocation Models . . . 445
12.1.1 Dip-slip faults . . . 446
12.2 Plate Motions . . . 450
12.3 Elastic Block Models . . . 452
12.4 Viscoelastic Cycle Models . . . 454
12.4.1 Viscoelastic Strike-Slip Earthquake Cycle Models . . . 454
12.4.2 Comparison to data from San Andreas Fault . . . 461
12.4.3 Viscoelastic Models with Stress Driven Deep Fault Creep . . . 465
12.4.4 Viscoelastic Cycle models For Dipping Faults . . . 474
12.5 Rate-State Friction Earthquake Cycle Models . . . 487
12.6 References . . . 491
12.7 Problems . . . 493

A Integral Transforms 495
A.1 Fourier Transforms . . . 495
A.2 Laplace Transforms . . . 497

B A Solution to the Diffusion Equation 501

C Solution of an Integral by Contour Methods 505